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## A Manager's Perspective

Renee Vaughn

Manager, Administration and Special Projects
Public and Media Relations
The Coca-Cola Company
I am responsible for providing scheduling and assisting with staffing with the Public and Media Relations group. This requires anticipating needs for the group and planning accordingly. I also administer budgets for three departments (about 35 employees).

I began my professional career in an elementary school district administration office, serving as an administrative assistant for the superintendent of schools. I learned to plan and manage budgets in that capacity. At The Coca-Cola Company, once a budget is created at the departmental level, it is tracked on a monthly basis by reviewing all spending by account and in total. We also review a rolling estimate of annual expenses and adjust the budget accordingly.

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## 5

# Cost-Volume-Profit Analysis 

Assume that a student organization wants to show movies on campus. The organization can rent a particular movie for one weekend for $\$ 1,000$. Rent for an auditorium, salaries for ticket takers and other personnel, and other fixed costs would amount to $\$ 800$ for the weekend. The organization would sell tickets for $\$ 4$ per person. In addition, profits from the sale of soft drinks, popcorn, and candy are estimated to be $\$ 1$ per ticket holder. How many people would have to buy tickets to justify renting the movie? (The answer is 360 ticket-buyers as shown in the solution to Demonstration Problem 5-B at the end of this chapter.)

Solving problems like this requires an understanding of the relationship between costs, revenue, and volume. This chapter discusses the use of cost-volumeprofit analysis for decision making and planning. (Although accountants call this topic cost-volume-profit analysis, it could just as easily have been called cost-volumerevenue analysis.) All of the analysis in this chapter is on a before-tax basis.

In this chapter we will focus on short-run decisions. The term short run describes a time frame during which a company's management cannot change the effects of certain past decisions. The short run is one year or less for practical purposes. For example, General Motors Corporation's decision to offer a special rebate starting January 5 and expiring on January 31 would be a short-run decision. In contrast, GM's decision to start the Saturn Corporation was a long-run decision.

In the short run, we assume many costs are fixed and unchangeable, such as building rental expense. However, all costs are subject to change in the long run. Although we identify particular costs as fixed in this chapter, you should realize that costs fixed in the short run may change in the long run. Someday the building rental agreement will change, so the building rental expense will change.

## Learning Objectives

After studying this chapter, you should be able to:

1. Explain and describe cost behavior patterns.
2. Separate mixed costs into fixed and variable components using the scatter diagram and high-low method.
3. Explain the relationship among costs, volume, revenue, and profits.
4. Find the break-even point.
5. Compute the margin of safety.
6. Demonstrate applications of cost-volume-profit analysis.
7. List the assumptions underlying cost-volumeprofit analysis.

## Objectives

8. Describe how computer spreadsheets expand your capability to use cost-volume-profit analysis.
9. Describe the impact of automation on fixed-variable cost relationships.

## Cost Behavior Patterns

Illustration 5.1 shows four basic cost behavior patterns: fixed, variable, mixed (semivariable), and step. As discussed in earlier chapters, fixed costs remain constant (in total) over some relevant range of output. Often, we describe them as time-related costs. Depreciation, insurance, property taxes, and administrative salaries are examples of fixed costs. Recall that so-called fixed costs are fixed in the short run but not necessarily in the long run.

For example, a local high-tech company did not lay off employees during a recent decrease in business volume because the management did not want to hire and train new people when business picked up again. Management treated direct labor as a fixed cost in this situation. Although volume decreased, direct labor costs remained fixed.

## Illustration 5.1 Four Cost Patterns

## Reinforcing Problem

E5-1 Match cost behavior types with diagrams


## Objective 1

Explain and describe cost behavior patterns.

In contrast to fixed costs, variable costs vary (in total) directly with changes in volume of production or sales. In particular, total variable costs change as total volume changes. If pizza production increases from 10010 -inch pizzas to 20010 -inch pizzas per day, the amount of dough required per day to make 10 -inch pizzas would double. The dough is a variable cost of pizza production. Direct materials and sales commissions are variable costs.

Direct labor is a variable cost in many cases. If the total direct labor cost increases as the volume of output increases and decreases as volume decreases, direct labor is a variable cost. Piecework pay is an excellent example of direct labor as a variable cost. In addition, direct labor is frequently a variable cost for workers paid on an hourly basis, as the volume of output increases, more workers are hired. However, sometimes the nature of the work or management policy does not allow direct labor to change as volume changes and direct labor can be a fixed cost.

Mixed costs have both fixed and variable characteristics. A mixed cost contains a fixed portion of cost incurred even when the facility is idle, and a variable portion that increases directly with volume. Electricity is an example of a mixed cost. A company must incur a certain cost for basic electrical service. As the company increases its volume of activity, it runs more machines and runs them longer. The firm also may extend its hours of operation. As activity increases, so does the cost of electricity.

Managers usually separate mixed costs into their fixed and variable components for decision-making purposes. They include the fixed portion of mixed costs with other fixed costs, while assuming the variable part changes with volume. Look at Illustration 5.2 to see how to separate the fixed and variable portions of a mixed cost such as electricity.

## Illustration 5.2 Separation of Mixed Costs into Fixed and Variable Parts



A step cost remains constant at a certain fixed amount over a range of output (or sales). Then, at certain points, the step costs increase to higher amounts. Visually, step costs appear like stair steps, as shown in Illustration 5.1.

Supervisors' salaries are an example of a step cost when companies hire additional supervisors as production increases. For instance, the local McDonald's restaurant has one supervisor until sales exceed 100 meals during the lunch hour. If sales regularly exceed 100 meals during that hour, the company adds a second supervisor. In Illustration 5.3, we show a step cost for supervisors' salaries, assuming each supervisor is paid $\$ 2,000$ per month. Step costs are sometimes labeled as step variable costs (many small steps) or step fixed costs (only a few large steps).

## McDonald's

McDonald's Corporation is an international fast-food restaurant chain.

Illustration 5.3 A Step Cost


Although we have described four different cost patterns (fixed, variable, mixed, and step), we simplify our discussions in this chapter by assuming managers can separate mixed and step costs into fixed and variable components.

## Curvilinear Cost Patterns

Many costs do not vary in a strictly linear relationship with volume. Rather, costs may vary in a curvilinear pattern-a $10 \%$ increase in volume may yield an $8 \%$ change in total variable costs at lower output levels and an $11 \%$ change in total variable costs at higher output levels. We show a curvilinear cost pattern in Illustration 5.4.

## Illustration 5.4 Curvilinear Cost Pattern



One way to deal with a curvilinear cost pattern is to assume a linear relationship between costs and volume within some relevant range. The relevant range is the range of production or sales volume over which the assumptions about cost behavior are valid. Look at Illustration 5.5 to see how to apply the relevant range to a portion of the curvilinear cost curve. Within that relevant range, the total cost varies linearly with volume, at least approximately. Outside of the relevant range, we presume the assumptions about cost behavior may be invalid.

## Illustration 5.5 Relevant Range



Costs rarely behave in the simple way that would make life easy for decision makers. Even within the relevant range, the assumed cost behavior is usually only approximately linear. As decision makers, we have to live with the fact that cost estimates are not as precise as physical or engineering measurements.

## Methods for Analyzing Costs

You can use several methods to break down a mixed cost into its fixed and variable cost components. We present two of these methods-the scatter diagram and the high-low method.

A scatter diagram shows plots of actual costs incurred for various levels of activity. Assume the dots on the scatter diagram in Illustration 5.6 represent total actual maintenance costs per month for a Federal Express fleet of delivery trucks. Each dot represents one month's activity for one city. For example, the left point represents a $\$ 38,000$ cost for approximately 30,000 miles a month. The next point to the right represents $\$ 42,000$ for approximately 40,000 miles for another month. We drew a line that appears to best fit the pattern of dots. The line we drew is subjective. ${ }^{1}$ If you were to draw such a line, your line would probably differ from ours.

Estimating fixed and variable costs using a scatter diagram is subjective. If your line through the dots in Illustration 5.6 differs from ours, you would estimate different fixed and variable costs. Your line and cost estimates would not necessarily be right or wrong compared to ours, just different.

## Scatter Diagram

## Objective 2

Separate mixed costs into fixed and variable components using the scatter diagram and high-low method.

## Illustration 5.6 Scatter Diagram



In Illustration 5.6, our line intersects the vertical axis at $\$ 25,000$, which we estimate to be the fixed portion of the mixed cost. We estimate the line would pass through a point representing a cost of $\$ 57,000$ at a volume of 80,000 miles. Thus, our line rises from $\$ 25,000$, representing 0 (zero) miles, to $\$ 57,000$ over a volume of 80,000 miles on the horizontal axis. Based on that information, we can now compute the variable cost portion of the mixed cost as follows:

$$
\frac{\$ 57,000-\$ 25,000}{80,000 \text { miles }-0 \text { miles }}=\$ 0.40 \text { per mile }
$$

[^0]
## High-Low Method

Reinforcing Problem
E5-2 Analyze mixed cost using high-low method

Using this result, we estimate the company's truck maintenance costs are $\$ 25,000$ per month plus 40 cents for every mile driven.

You can also use the high-low method to identify the elements of mixed costs. This method uses only the highest and lowest points (levels of operation) on a scatter diagram to fit a line to the data.

To illustrate, the lowest point in Illustration 5.6, is $\$ 38,000$ of expense at 30,000 miles driven, and the highest point is $\$ 60,000$ at 80,000 miles. Calculate the amount of variable cost per mile as follows:
$\frac{\text { Change in cost }}{\text { Change in units }}=\frac{\$ 60,000-\$ 38,000}{80,000 \text { miles }-30,000 \text { miles }}=\frac{\$ 22,000}{50,000 \text { miles }}=\$ 0.44$ per mile
To compute the fixed portion:

Total cost at 80,000 miles
\$60,000
Less: Variable cost at that level of output $(80,000 \times \$ 0.44)$
Fixed cost at all levels of mileage within the relevant range
\$24,800

The high-low method is less precise than the scatter diagram because it uses only two data points in the computation. Either or both points may not be representative of the data as a whole.

Many people use more sophisticated statistical techniques to divide mixed costs into fixed and variable portions. Statistics and cost accounting texts discuss these techniques.

Now that you understand cost patterns and how to analyze costs, we will apply these concepts to the specific tools that managers use in short-term decision making. The first of these tools is cost-volume-profit (CVP) analysis.

## Cost-Volume-Profit (CVP) Analysis

Companies use cost-volume-profit (CVP) analysis (also called break-even analysis) to determine what affects changes in their selling prices, costs, and/or volume will have on profits in the short run. A careful and accurate cost-volume-profit (CVP) analysis requires knowledge of costs and their fixed or variable behavior as volume changes.

Cost-Volume-Profit Chart

A cost-volume-profit chart is a graph that shows the relationships among sales, costs, volume, and profit. Look at Illustration 5.7, a cost-volume-profit chart for Video Productions, a company that produces videotapes. Each tape sells for $\$ 20$. The variable cost per tape is $\$ 12$, and the fixed costs per month are $\$ 40,000$.

The total cost line in Illustration 5.7 represents the fixed costs of $\$ 40,000$ plus $\$ 12$ per unit. Thus, if Video Productions produces and sells 6,000 tapes, the company's total costs are $\$ 112,000$, made up of $\$ 40,000$ fixed costs and $\$ 72,000$ total variable costs $(\$ 72,000=\$ 12$ per unit $\times 6,000$ units produced and sold $)$.

The total revenue line in Illustration 5.7 shows how revenue increases as volume increases. Total revenue is $\$ 120,000$ for sales of 6,000 tapes $(\$ 120,000=\$ 20$ per unit $\times 6,000$ units sold). In Illustration 5.7 , we demonstrate the effect of volume on revenue, costs, and net income, for a particular price, variable cost per unit, and fixed cost per period.


At each volume, one can estimate the company's profit or loss. For example, at a volume of 6,000 units, the profit is $\$ 8,000$. We can find the net income either by constructing an income statement or using the profit equation. The income statement gives the following results for a volume of 6,000 units:


We have introduced a new term in this income statement-the contribution margin. The contribution margin is the amount by which revenue exceeds the variable costs of producing that revenue. We can calculate it on a per unit or total sales volume basis. On a per unit basis, the contribution margin for Video Productions is $\$ 8$ (the selling price of $\$ 20$ minus the variable cost per unit of $\$ 12$ ).

The contribution margin indicates the amount of money remaining after the company covers its variable costs. This remainder contributes to the coverage of fixed costs and to net income. In Video Production's income statement, the $\$ 48,000$ contribution margin covers the $\$ 40,000$ fixed costs and leaves $\$ 8,000$ in net income.

Profit Equation The profit equation is just like the income statement, except it presents the analysis in a slightly different form. According to the profit equation:

$$
\text { Net income }=\text { Revenue }- \text { Total variable costs }- \text { Fixed costs }
$$

For Video Productions, the profit equation looks like this:

$$
\begin{aligned}
& \text { Net income }=\$ 120,000-\$ 72,000-\$ 40,000 \\
& \text { Net income }=\$ 8,000
\end{aligned}
$$

Objective 4
Find the break-even point.

Reinforcing Problem
E5-4 Compute break-even point in units

Illustration 5.7 shows cost data for Video Productions in a relevant range of output from 500 to 10,000 units. Recall the relevant range is the range of production or sales volume over which the basic cost behavior assumptions hold true. For volumes outside these ranges, costs behave differently and alter the assumed relationships. For example, if Video Productions produced and sold more than 10,000 units per month, it might be necessary to increase plant capacity (thus incurring additional fixed costs) or to work extra shifts (thus incurring overtime charges and other inefficiencies). In either case, the assumed cost relationships would no longer be valid.

## Finding the Break-Even Point

A company breaks even for a given period when sales revenue and costs charged to that period are equal. Thus, the break-even point is that level of operations at which a company realizes no net income or loss.

A company may express a break-even point in dollars of sales revenue or number of units produced or sold. No matter how a company expresses its break-even point, it is still the point of zero income or loss. To illustrate the calculation of a break-even point, recall that Video Productions produces videotapes selling for $\$ 20$ per unit. Fixed costs per period total $\$ 40,000$, while variable cost is $\$ 12$ per unit.

Break-Even in Units We compute the break-even point in units by dividing total fixed costs by the contribution margin per unit. The contribution margin per unit is $\$ 8$ ( $\$ 20$ selling price per unit - $\$ 12$ variable cost per unit). In the following break-even equation, BE refers to the break-even point:

$$
\begin{aligned}
\mathrm{BE}_{\text {units }} & =\frac{\text { Fixed costs }}{\text { Contribution margin per unit }} \\
\mathrm{BE}_{\text {units }} & =\frac{\$ 40,000}{\$ 8 \text { per unit }} \\
\mathrm{BE}_{\text {units }} & =5,000 \text { units }
\end{aligned}
$$

The result tells us that Video Productions breaks even at a volume of 5,000 units per month. We can prove that to be true by computing the revenue and total costs at a volume of 5,000 units. Revenue $=5,000$ units $\times \$ 20$ sales price per unit $=\$ 100,000$. Total costs $=\$ 100,000=\$ 40,000$ fixed costs $+\$ 60,000$ variable costs $(\$ 60,000=\$ 12$ per unit $\times 5,000$ units).

Look at Illustration 5.7 and note that the revenue and total cost lines cross at 5,000 units-the break-even point. Video Productions has net income at volumes greater than 5,000 , but it has losses at volumes less than 5,000 units.

Break-Even in Sales Dollars Companies frequently think of volume in sales dollars instead of units. For a company such as General Motors that makes Cadillacs and spark plugs, it makes no sense to think of a break-even point in units. GM breaks even in sales dollars.

The formula to compute the break-even point in sales dollars looks a lot like the formula to compute the break-even in units, except we divide fixed costs by the contribution margin ratio instead of the contribution margin per unit.

$$
\mathrm{BE}_{\text {dollars }}=\frac{\text { Fixed costs }}{\text { Contribution margin ratio }}
$$

The dean of the Business School at a particular university was considering whether to offer a particular seminar for executives. The tuition would be $\$ 650$ per person. Variable costs, including meals, parking, and materials, would be $\$ 80$ per person. Certain costs of offering the seminar, including advertising, instructors' fees, room rent, and audiovisual equipment rent, would not be affected by the number of people attending (within a "relevant range"). Such costs, which could be thought of as fixed costs, amounted to $\$ 8,000$ for the seminar.

In addition to these costs, a number of staff, including the dean, would work on the program. Although the salaries paid to these staff were not affected by offering the seminar, working on it took these people away from other duties, thus creating an opportunity cost, estimated to be $\$ 7,000$ for this seminar.

Given this information, the school estimated the break-even point to be (\$8,000 $+\$ 7,000) /(\$ 650-\$ 80)=26.3$ students. If the school wanted at least to break even on this program, it should offer the program only if it expected at least 27 students to attend. Based on the authors' research.

## A Broader Perspective

## Even Colleges Use CVP

The contribution margin ratio expresses the contribution margin as a percentage of sales. To calculate this ratio, divide the contribution margin per unit by the selling price per unit, or total contribution margin by total revenues. Video Production's contribution margin ratio is:

$$
\begin{aligned}
\text { Contribution margin ratio } & =\frac{\text { Contribution margin per unit }}{\text { Selling price per unit }} \\
& =\frac{\$ 20-\$ 12}{\$ 20}=\frac{\$ 8}{\$ 20} \\
& =0.40
\end{aligned}
$$

Or, referring to the income statement in which Video Productions had a total contribution margin of $\$ 48,000$ on revenues of $\$ 120,000$, we compute the contribution margin ratio as follows:

$$
\begin{aligned}
\text { Contribution margin ratio } & =\frac{\text { Total contribution margin }}{\text { Total revenues }} \\
& =\frac{\$ 48,000}{\$ 120,000} \\
& =0.40
\end{aligned}
$$

That is, for each dollar of sales, there is a $\$ 0.40$ contribution to covering fixed costs and generating net income.

Using this ratio, we calculate Video Production's break-even point in sales dollars as:

## Reinforcing Problem

E5-3 and E5-5 Compute break-even point in sales dollars

$$
\begin{aligned}
\mathrm{BE}_{\text {dollars }} & =\frac{\text { Fixed costs }}{\text { Contribution margin ratio }} \\
\mathrm{BE}_{\text {dollars }} & =\frac{\$ 40,000}{0.40} \\
& =\$ 100,000
\end{aligned}
$$

## Reinforcing Problem

E5-6 Compute break-even point in sales dollars and units under varying assumptions; comment on results

Calculating Break-Even for a Multiproduct Company

The break-even volume of sales is $\$ 100,000$ (5,000 units at $\$ 20$ per unit). At this level of sales, fixed costs plus variable costs equal sales revenue, as shown here:

Revenues<br>Less: variable costs<br>Contribution margin<br>Less: Fixed costs<br>Net income



The cost-volume-profit chart in Illustration 5.7 shows that in a period of complete idleness, Video Productions would lose $\$ 40,000$ (the amount of fixed costs). However, when Video Productions has an output of 10,000 units, the company has net income of $\$ 40,000$. Other points on the graph show that sales of 7,500 units results in $\$ 150,000$ of revenue. At that point, Video Production's total costs amount to $\$ 130,000$, leaving net income of $\$ 20,000$.

Although you are likely to use cost-volume-profit analysis for a single product, you will more frequently use it in multiproduct situations. The easiest way to use cost-volume-profit analysis for a multiproduct company is to use dollars of sales as the volume measure. For CVP purposes, a multiproduct company must assume a given product mix. Product mix refers to the proportion of the company's total sales attributable to each type of product sold.

To illustrate the computation of the break-even point for Wonderfood, a multiproduct company that makes three types of cereal, assume the following historical data:

| Product |  |  |  |  |  | Total |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | 2 |  | 3 |  |  |  |
| Amount | Percent | Amount | Percent | Amount | Percent | Amount | Percent |
| \$60,000 | 100\% | \$30,000 | 100\% | \$10,000 | 100\% | \$100,000 | 100\% |
| 40,000 | 67\% | 16,000 | 53\% | 4,000 | 40\% | 60,000 | 60\% |
| \$20,000 | 33\% | \$14,000 | 47\% | \$6,000 | 60\% | \$ 40,000 | 40\% |

We use the data in the total columns to compute the break-even point. The contribution margin ratio is $40 \%$ or $(\$ 40,000 / \$ 100,000)$. Assuming the product mix remains constant and fixed costs for the company are $\$ 50,000$, break-even sales are $\$ 125,000$, computed as follows:

$$
\begin{aligned}
\mathrm{BE}_{\text {dollars }} & =\frac{\text { Fixed costs }}{\text { Contribution margin ratio }} \\
\mathrm{BE}_{\text {dollars }} & =\frac{\$ 50,000}{0.40} \\
& =\$ 125,000
\end{aligned}
$$

[To check our answer: $(\$ 125,000 \times 0.40)-\$ 50,000=\$ 0$.]
To find the three product sales totals, we multiply total sales dollars by the percent of product mix for each of the three products. The product mix for products 1 , 2 , and 3 is $60: 30: 10$, respectively. That is, out of the $\$ 100,000$ total sales, there were sales of $\$ 60,000$ for product $1, \$ 30,000$ for product 2 , and $\$ 10,000$ for product 3 . Therefore, the company has to sell $\$ 75,000$ of product $1(0.6 \times \$ 125,000), \$ 37,500$ of product $2(0.3 \times \$ 125,000)$, and $\$ 12,500$ of product $3(0.1 \times \$ 125,000)$ to break even.

Business Insight The founder of Domino's Pizza, Inc., nearly went bankrupt several times before he finally made Domino's a financial success. One early problem was that the company was providing small pizzas that cost almost as much to make and just as much to deliver as larger pizzas. Because they were small, the company could not charge enough to cover its costs. At one point, the company's founder was so busy producing small pizzas that he did not have time to determine that the company was losing money on them.

If a company's current sales are more than its break-even point, it has a margin of safety equal to current sales minus break-even sales. The margin of safety is the amount by which sales can decrease before the company incurs a loss. For example, assume Video Productions currently has sales of $\$ 120,000$ and its break-even sales are $\$ 100,000$. The margin of safety is $\$ 20,000$, computed as follows:

$$
\begin{aligned}
\text { Margin of safety } & =\text { Current sales }- \text { Break-even sales } \\
& =\$ 120,000-\$ 100,000 \\
& =\$ 20,000
\end{aligned}
$$

Sometimes people express the margin of safety as a percentage, called the margin of safety rate. The margin of safety rate is equal to (Current sales - Breakeven sales)/Current sales. Using the data just presented, we compute the margin of safety rate as follows:

$$
\begin{aligned}
\text { Margin of safety rate } & =\frac{\text { Current sales }- \text { Break-even sales }}{\text { Current sales }} \\
& =\frac{\$ 120,000-\$ 100,000}{\$ 120,000} \\
& =16.67 \%
\end{aligned}
$$

This means that sales volume could drop by $16.67 \%$ before the company would incur a loss.

## Cost-Volume-Profit Analysis Illustrated

CVP analysis has many applications. This section illustrates several applications using airline data.

The management of a major airline wishes to know how many seats must be sold on Flight 529 to break even. To solve this problem, management must identify and separate costs into fixed and variable categories.

The fixed costs of Flight 529 are the same regardless of the number of seats filled. Fixed costs include the fuel required to fly the plane and crew (with no passengers) to its destination; depreciation on the plane used on the flight; and salaries of required crew members, gate attendants, and maintenance and refueling personnel.

## An Accounting Perspective

Margin of Safety

## Objective 5

Compute the margin of safety.

## Reinforcing Problem

E5-7 Decide whether to increase advertising; compute margin of safety

Objective 6
Demonstrate applications of cost-volume-profit analysis.

Calculating
the Break-Even
Point

The variable costs vary directly with the number of passengers. Variable costs include snacks and beverages provided to passengers, baggage handling costs, and the cost of the additional fuel required to fly the plane with passengers to its destination. Management would express each variable cost on a per passenger basis.

Assume that after analyzing the various costs and separating them into fixed or variable categories, management finds the fixed costs for Flight 529 are $\$ 12,000$ and variable costs are $\$ 25$ per passenger. Tickets cost $\$ 125$. Thus, the contribution margin ratio is $80 \%$ or [( $\$ 125-\$ 25) / \$ 125]$.

We can express the break-even point either in sales dollars or in the number of passengers. The break-even point in sales dollars is:

$$
\begin{aligned}
\mathrm{BE}_{\text {dollars }} & =\frac{\text { Fixed costs }}{\text { Contribution margin ratio }} \\
& =\frac{\$ 12,000}{0.80} \\
& =\$ 15,000
\end{aligned}
$$

We can find the break-even point in number of passengers (units) by dividing fixed costs by the contribution margin per unit:

$$
\begin{aligned}
\mathrm{BE}_{\text {units }} & =\frac{\text { Fixed costs }}{\begin{array}{c}
\text { Contribution margin per unit } \\
\text { (or passenger) }
\end{array}} \\
& =\frac{\$ 12,000}{\$ 125-\$ 25} \\
& =120 \text { passengers }
\end{aligned}
$$

To check our answers: 120 passengers $\times \$ 125$ ticket price $=\$ 15,000$.

## Calculating Sales Volume Needed for Desired Net Income

## Reinforcing Problem

E5-9 Compute break-even points to achieve a specified level of income

With a simple adjustment in the break-even formulas, CVP analysis can also show the sales volume needed to generate some desired level of net income (ignore taxes). To make this adjustment, management adds the desired net income amount to the fixed costs that must be covered. From this, management can determine the necessary sales volume in dollars or units to provide the desired net income. For example, assume management wishes to earn $\$ 8,000$ of net income on Flight 529.

How many passenger tickets must the airline sell to earn $\$ 8,000$ ? Remember, the contribution margin per ticket is $\$ 100$. We compute the number of tickets to be sold to earn $\$ 8,000$ on a flight as follows:

$$
\begin{aligned}
\text { Number of units } & =\frac{\text { Fixed costs }+ \text { Desired net income }}{\text { Contribution margin per unit }} \\
& =\frac{\$ 12,000+\$ 8,000}{\$ 100} \\
& =\frac{\$ 20,000}{\$ 100} \\
& =200 \text { tickets }
\end{aligned}
$$

The airline must sell 200 tickets to earn net income of $\$ 8,000$. To check our answer: ( 200 tickets $\times \$ 125$ sales price per ticket) - (200 tickets $\times \$ 25$ variable cost per ticket) $-\$ 12,000$ fixed costs $=\$ 25,000-\$ 5,000-\$ 12,000=\$ 8,000$.

The airline management can also use cost-volume-profit analysis to determine the effect of changing the sales price. To illustrate, assume that Flight 529 normally carries 150 passengers (sales of $\$ 18,750$ and net income of $\$ 3,000$ ), and the airline decides to increase ticket prices by $5 \%$. If variable and fixed costs remain constant and passenger load does not change, net income increases from $\$ 3,000$ to $\$ 3,937.50$ as follows:

Revenue - Total variable costs - Fixed costs $=$ Net income

$$
\begin{aligned}
& {[\$ 125(1.05) \times 150 \text { passengers }]-} \\
&(\$ 25 \times 150 \text { passengers })-\$ 12,000=\mathrm{NI} \\
& \$ 19,687.50-\$ 3,750-\$ 12,000=\mathrm{NI} \\
& \$ 19,687.50-\$ 15,750=\mathrm{NI} \\
& \$ 3,937.50=\mathrm{NI}
\end{aligned}
$$

Net income would rise by the entire amount of the price increase (\$19,687.50-\$18,750 $=\$ 937.50$ ).

Management can use cost-volume-profit analysis to calculate the sales needed to maintain net income when costs change. For example, assume both fixed and variable costs would increase for the airline if the price of fuel rises. Assume that fixed costs increase by $\$ 4,000$ and variable costs increase by $\$ 6.25$ per passenger. Variable costs are now $25 \%$, or ( $\$ 31.25 /$ $\$ 125$ ), of the sales price. The contribution margin is now $\$ 93.75$, or ( $\$ 125-\$ 31.25$ ), per passenger. The contribution margin ratio is now $75 \%$, or $(\$ 93.75 / \$ 125)$.

To maintain the current net income of $\$ 3,000$, the airline needs to increase sales revenue to $\$ 25,333$ :

$$
\begin{aligned}
\text { Revenue required } & =\frac{\text { Fixed costs }+ \text { Desired net income }}{\text { Contribution margin ratio }} \\
& =\frac{\$ 16,000+\$ 3,000}{0.75} \\
& =\$ 25,333
\end{aligned}
$$

Management can also use its knowledge of cost-volume-profit relationships to determine whether to increase sales promotion costs in an effort to increase sales volume or to accept an order at a lower-than-usual price. In general, the careful study of cost behavior helps management plan future courses of action.

## Calculating the

 Effect of Changing the Sales Price on Net IncomeCalculating Sales Needed to Maintain Net Income When Costs Change

## A Broader Perspective

Major Television Networks Are Finding It Harder to Break Even

With increasing competition from cable television, prerecorded videos, and independent stations, the three major television networks are facing smaller and smaller margins of safety. Most new shows do not break even. Many do not even cover their variable costs and are dropped during the first season.

As the networks find it more and more difficult to break even on their regular shows, they are expanding into cable, satellite, and pay-per-view television. For example, the National Broadcasting Company (NBC), a major television network owned by General Electric Company, is part owner of a national cable channel and a sports channel. The company has also invested in CNBC, a cable network that specializes in consumer and business issues.
Based on the authors' research.

## Assumptions Made in Cost-Volume-Profit Analysis

To summarize, the most important assumptions underlying CVP analysis are:

1. Selling price, variable cost per unit, and total fixed costs remain constant through the relevant range. This means that a company can sell more or fewer units at the same price and that the company has no change in technical efficiency as volume changes.
2. In multiproduct situations, the product mix is known in advance.
3. Costs can be accurately classified into their fixed and variable portions.

Critics may call these assumptions unrealistic in many situations, but they greatly simplify the analysis.

## Using Computer Spreadsheets for CVP Analysis

Computer spreadsheet packages are well suited for CVP analysis because they enable managers to answer what-if questions. The cost and revenue items in CVP analysis are estimates, not actual results. Since they are used in planning and decision making, it is reasonable to ask whether plans or decisions would change if the estimates changed. The most important issue is whether the information is correct. The output is only as good as the information that goes in.

Consider the following example: The management of Prince Cruises wants to know what the income before taxes would be for a proposed product, a Caribbean cruise. The analyst prepared the following formulas for the spreadsheet:

- Revenue equals ticket price times number of passengers (amounts to be inserted for ticket price and number of passengers).
Contribution margin equals (amount to be inserted)\% of revenue.
Fixed costs equal $\$ 200,000$.
Income equals revenue minus variable costs minus fixed costs.
Management then inserted various values for ticket price, number of passengers, the percent of variable cost to revenue, and fixed costs, all per cruise. Illustration 5.8 shows the results. Based on these results, management sees what combinations of ticket price, number of passengers, and contribution ratio are required for the cruise to be profitable.

We show only a few of the possible combinations in Illustration 5.8 to save space. Spreadsheets provide the advantage of a large number of possible combinations with minimal data entry.

## Illustration 5.8 Spreadsheet Analysis of CVP Relationships

| Fixed Cost | Ticket Price | Number of <br> Passengers | Percent Contribution <br> Margin to Revenue | Income |
| :---: | :---: | :---: | :---: | :---: |
| $\$ 200,000$ | $\$ 3,000$ | 100 | $70 \%$ | $\$ 10,000$ |
| 200,000 | 3,000 | 80 | $70 \%$ | $(32,000)$ |
| 200,000 | 3,000 | 100 | $75 \%$ | 25,000 |
| 200,000 | 3,000 | 80 | $75 \%$ | $(20,000)$ |
| 200,000 | 4,000 | 70 | $70 \%$ | $(4,000)$ |
| 200,000 | 4,000 | 50 | $70 \%$ | $(60,000)$ |
| 200,000 | 4,000 | 70 | $75 \%$ | 10,000 |
| 200,000 | 4,000 | 50 | $75 \%$ | $(50,000)$ |

Uses of Technology Cost-volume-profit analysis using a computer spreadsheet is becoming routine. In many business meetings, we find one or more people crunching cost-volume-profit numbers on their notebook or laptop computers.

## An Accounting Perspective

## Effect of Automation on Cost-Volume-Profit Analysis

Increasing automation does not affect the fundamental CVP model or the types of analysis we have discussed. However, it does affect the relative size of fixed and variable costs. As companies become more automated, they substitute machinery for labor. Companies that make this substitution often increase fixed costs and decrease variable costs. For example, when banks installed automated teller machines, their labor costs decreased but their fixed costs, including machine depreciation, increased.

When a company substitutes fixed costs for variable costs, the total cost line shifts up as shown in Illustration 5.9. At low levels of volume, becoming more automated increases total costs, but at high levels of volume it decreases them. What does this do to the company's break-even point? It depends on where the revenue line crosses the total cost line.

## Objective 9

Describe the impact of automation on fixed-variable cost relationships.

## Illustration 5.9 Effects of Automation



If it crosses at low volumes, to the left of point A in Illustration 5.9, then increasing automation increases the company's break-even point. At high volumes, however, if increasing automation lowers total costs, it lowers the company's break-even point.

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[^1]In this chapter we began studying short-run decisions based on cost-volumeprofit analysis. In Chapter 6 we will apply differential analysis to short-term decisions.

## Understanding the Learning Objectives

## Objective 1

Explain and describe cost behavior patterns.

## Objective 2

Separate mixed costs into fixed and variable components using the scatter diagram and high-low method.

## Objective 3

Explain the relationship among costs, volume, revenue, and profits.

## Objective 4

Find the break-even point.

- Fixed costs. These costs remain constant in total over some relevant range of output and are often described as time-related costs. Depreciation and insurance are examples.
- Variable costs. These costs vary in total directly with changes in the volume of production or sales. Direct materials and sales commissions are examples.
- Mixed costs. These costs contain a fixed portion of cost incurred even when the plant is completely idle and a variable portion that increases directly with production volume. Electricity is an example of a mixed cost.
- Step costs. These costs remain constant at a certain fixed amount over a short range of output (or sales) but increase to higher amounts at certain points. The cost of supervisors' salaries is an example.
- The scatter diagram shows plots of actual costs incurred for various levels of activity.
- The high-low method uses the highest and lowest points on a scatter diagram to fit a line to the data.
- Cost-volume-profit analysis (sometimes called break-even analysis) can determine what effects any changes in a company's selling prices, costs, and/or volume will have on net income in the short run.
- The break-even point is that level of operations at which a company realizes no income or loss.
- To compute the break-even point in sales dollars:

$$
\mathrm{BE}_{\text {dollars }}=\frac{\text { Fixed costs }}{\text { Contribution margin ratio }}
$$

Or, to express the break-even point in units:

$$
\mathrm{BE}_{\text {umis }}=\frac{\text { Fixed costs }}{\text { Contribution margin per unit }}
$$

- To compute the margin of safety:


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- Applications include calculation of the break-even point, calculation of the sales volume needed for a desired net income, calculation of the effect of changing price on net income, and calculation of the sales needed to maintain net income when costs change.
- Selling price, variable cost per unit, and total fixed costs remain constant through the relevant range.
- In multiproduct situations, the product mix is known in advance.
- Costs can be accurately classified into their fixed and variable portions.
- Computer spreadsheet packages are well suited for CVP analysis because they enable managers to answer what-if questions.
- As companies become more automated, they substitute machinery for labor, which generally increases fixed costs and decreases variable costs.


## Demonstration Problem 5-A

Davis Company has fixed costs of $\$ 625,000$ per year and variable costs of $\$ 7.50$ per unit. Its product sells for $\$ 12.50$ per unit. Full capacity is 200,000 units. The contribution margin is $\$ 5$ per unit ( $\$ 12.50-\$ 7.50)$.
a. Compute the break-even point in (1) sales dollars and (2) units.
b. Compute the number of units the company must sell if it wishes to have net income of $\$ 300,000$.

## Solution to Demonstration Problem 5-A

a. (1) The contribution margin ratio is 0.40 .

$$
\begin{aligned}
\mathrm{BE}_{\text {dollars }} & =\frac{\text { Fixed costs }}{\text { Contribution margin ratio }} \\
\mathrm{BE}_{\text {dollars }} & =\frac{\$ 625,000}{0.40} \\
& =\$ 1,562,500
\end{aligned}
$$

## Objective 6

Demonstrate applications of cost-volume-profit analysis.

## Objective 7

List the assumptions underlying cost-volume-profit analysis.

## Objective 8

Describe how computer spreadsheets expand your capability to use cost-volume-profit analysis.

## Objective 9

Describe the impact of automation on fixed-variable cost relationships.
(2)

$$
\begin{aligned}
\mathrm{BE}_{\text {units }} & =\frac{\text { Fixed costs }}{\text { Contribution margin per unit }} \\
\mathrm{BE}_{\text {units }} & =\frac{\$ 625,000}{\$ 5} \\
& =125,000 \text { units }
\end{aligned}
$$

b.

$$
\begin{aligned}
\text { Number of units } & =\frac{\text { Fixed cost }+ \text { Desired net income }}{\text { Contribution margin per unit }} \\
& =\frac{\$ 625,000+\$ 300,000}{\$ 5} \\
& =\frac{\$ 925,000}{\$ 5} \\
& =185,000 \text { units }
\end{aligned}
$$

## Demonstration Problem 5-B

At the beginning of this chapter, we presented a problem: A campus organization wants to show movies. Recall that the movie rental would be $\$ 1,000$. Rent for an auditorium, salaries to the ticket takers and other personnel, and other fixed costs would be $\$ 800$ for the weekend. The organization would sell tickets for $\$ 4$ per person. In addition, profits from the sale of soft drinks, popcorn, and candy are estimated to be $\$ 1$ per ticket holder. How many people have to buy tickets for the organization to break even?

## Solution to Demonstration Problem 5-B

$$
\begin{aligned}
\text { Number of ticket buyers to break even } & =\frac{\$ 1,000+\$ 800}{\$ 4+\$ 1} \\
& =\frac{\$ 1,800}{\$ 5} \\
& =360 \text { ticket buyers }
\end{aligned}
$$

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## New Terms*

Break-even point That level of operations at which revenues for a period are equal to the costs assigned to that period so there is no net income or loss. 142
Contribution margin The amount by which revenue exceeds the variable costs of producing that revenue. The contribution margin per unit is the selling price minus the variable cost per unit. 141
Contribution margin ratio Contribution margin per unit divided by selling price per unit, or total contribution margin divided by total revenues. 143
Cost-volume-profit (CVP) analysis An analysis of the effect that any changes in a company's selling prices, costs, and/or volume will have on income (profits) in the short run. Also called break-even analysis. 140
Cost-volume-profit (CVP) chart A graph that shows the relationships among sales, volume, costs, and net income or loss. 140
Fixed costs Costs that remain constant (in total) over some relevant range of output. 136
High-low method A method used in dividing mixed costs into their fixed and variable portions. The high plot and low plot of actual costs are used to draw a line representing a total mixed cost. 140
Margin of safety Amount by which sales can decrease before a loss is incurred. 145
Margin of safety rate Margin of safety expressed as a percentage, which equals (Current sales - Break-even sales)/Current sales. 145

Mixed cost Contains a fixed portion of cost incurred even when the plant is completely idle and a variable portion that increases directly with production volume. 136
Product mix The proportion of the company's total sales attributable to each type of product sold. 144
Profit equation The equation is Net income $=$ Revenue - Total variable costs - Fixed costs. 141
Relevant range The range of production or sales volume over which the assumptions about cost behavior are valid. 138
Scatter diagram A diagram that shows plots of actual costs incurred for various levels of activity; it is used in dividing mixed costs into their fixed and variable portions. 139
Short run The time during which a company's management cannot change the effects of certain past decisions; often determined to be one year or less. In the short run, many costs are assumed to be fixed and unchangeable. 135
Step cost A cost that remains constant at a certain fixed amount over a range of output (or sales) but then keeps increasing to a higher amount at certain points. 137
Variable costs Costs that vary (in total) directly with changes in the volume of production or sales. 136
*Some terms listed in earlier chapters are repeated here for your convenience.

## Self-Test

## True-False

Indicate whether each of the following statements is true or false.

1. The scatter diagram method is less precise than the high-low method for evaluating costs.
2. A break-even point is expressed only in dollars of sales revenues.
3. Total contribution margin indicates the amount of money remaining after variable and fixed costs are covered.
4. The margin of safety is calculated using the following formula:
Margin of safety $=$ Break-even sales - Current sales
5. Dollars of sales are used when computing the break-even point for a multiproduct company.

## Multiple-Choice

Select the best answer for each of the following questions.

1. Under which of the following cost behavior patterns would electricity be categorized?
a. Variable cost.
b. Fixed cost.
c. Mixed cost.
d. Step cost.
2. Which of the following are characteristics of step costs?
a. A fixed component.
b. Costs increase in steps as production volume increases.
c. Can remain constant over some relevant range of output.
d. All of the above.
3. Using the following data, calculate the sales revenue needed to break even:

| Selling price per unit | $\$ 10$ |
| :--- | ---: |
| Fixed costs | 20,000 |
| Variable cost per unit | 6 |

a. $\$ 40,000$.
b. $\$ 33,333$.
c. $\$ 50,000$.
d. $\$ 60,000$.
4. Using the following data, calculate the contribution margin:
Selling price
Fixed costs 4
Variable cost
a. $\$ 14$.
b. $\$ 10$.
c. $\$ 16$.
d. $\$ 18$.
5. Using the following data, calculate the break-even point in units:

| Selling price per unit | $\$ 20$ |
| :--- | ---: |
| Fixed costs | 28,000 |
| Variable cost per unit | 6 |

a. 1,400 units.
b. 2,800 units.
c. 2,275 units.
d. 2,000 units.
6. Which of the following describe(s) the underlying assumptions of cost-volume-profit analysis?
a. Selling price, variable cost per unit, and total fixed costs remain constant through the relevant range.
b. In multiproduct situations, the product mix is known in advance.
c. Costs can be accurately classified into their fixed and variable portions.
d. All of the above.

Now turn to page 164 to check your answers.

## Questions

1. Name and describe four cost behavior patterns.
2. Describe two methods of determining the fixed and variable components of mixed costs.
3. What is meant by the term break-even point?
4. What are two ways in which the break-even point can be expressed?
5. What is the relevant range?
6. What is the formula for calculating the breakeven point in sales revenue?
7. What formula is used to solve for the break-even point in units?
8. How can the break-even formula be altered to calculate the number of units that must be sold to achieve a desired level of income?
9. Why might a business wish to lower its breakeven point? How would it go about lowering the break-even point?
10. What effect would you expect the mechanization and automation of production processes to have on the break-even point?
11. Real World Question Assume your college is considering hiring a lecturer to teach a special class in communication skills. Identify at least two costs that college administrators might consider in deciding whether to hire the lecturer and add the class.
12. Real World Question Two enterprising students are considering renting space and opening a class videotape service. They would hire camera operators to videotape large introductory classes. The students taking the classes would be charged a fee to rent the tape or to view it on one of the service's television sets. Identify as many costs of this business as you can and indicate which would be variable and which would be fixed.

## Exercises

Name and match the types of cost behavior with the appropriate diagram below.


Match cost behavior types with diagrams (L.O. 1)

Exercise 5-2
Analyze mixed cost using high-low method (L.O. 2)

Exercise 5-3
Compute break-even point in sales dollars
(L.O. 4)

Exercise 5-4
Compute break-even point in units (L.O. 4)

Exercise 5-5
Compute break-even point in sales dollars
(L.O. 4)

## Volume (units)

Cost
\$70,000 190,000

## Exercise 5-6

Compute break-even point in sales dollars and units under varying assumptions; comment on results (L.O. 3, 4)

## Exercise 5-7

Decide whether to increase advertising; compute margin of safety (L.O. 3, 5)

## Exercise 5-8

Compute multiproduct break-even point and margin of safety (L.O. 4, 5)

Never Late Delivery currently delivers packages for $\$ 9$ each. The variable cost is $\$ 3$ per package, and fixed costs are $\$ 60,000$ per month. Compute the break-even point in both sales dollars and units under each of the following independent assumptions. Comment on why the break-even points are different.
a. The costs and selling price are as just given.
b. Fixed costs are increased to $\$ 75,000$.
c. Selling price is increased by $10 \%$. (Fixed costs are $\$ 60,000$.)
d. Variable cost is increased to $\$ 4.50$ per unit. (Fixed costs are $\$ 60,000$ and selling price is \$9.)

Best Eastern Motel is a regional motel chain. Its rooms rent for $\$ 100$ per night, on average. The variable cost is $\$ 40$ a room per night. Fixed costs are $\$ 5,000,000$ per year. The company currently rents 200,000 units per year, with each unit defined as one room for one night. Should this company undertake an advertising campaign resulting in a $\$ 500,000$ increase in fixed costs per year, no change in variable cost per unit, and a $10 \%$ increase in revenue (resulting from an increase in the number of rooms rented)? What is the margin of safety before and after the campaign?

Fall-For-Fun Company sells three products. Last year's sales were $\$ 600,000$ for parachutes, $\$ 800,000$ for hang gliders, and $\$ 200,000$ for bungee jumping harnesses. Variable costs were: parachutes, $\$ 400,000$; hang gliders, $\$ 700,000$; and bungee jumping harnesses, $\$ 100,000$. Fixed costs were $\$ 240,000$. Find ( a ) the break-even point in sales dollars and ( b ) the margin of safety.

Early Horizons Day Care Center has fixed costs of $\$ 300,000$ per year and variable costs of $\$ 10$ per child per day. If it charges $\$ 25$ a child per day, what will be its break-even point expressed in dollars of revenue? How much revenue would be required for Early Horizons Day Care to earn $\$ 100,000$ net income per year?

## Problems

Assume the local franchise of Togorio Sandwich Company assigns you the task of estimating total maintenance cost on its delivery vehicles. This cost is a mixed cost. You receive the following data from past months:

| Month | Units | Costs |
| :--- | ---: | ---: |
| March | 8,000 | $\$ 14,000$ |
| April | 10,000 | 14,960 |
| May | 9,000 | 15,200 |
| June | 11,000 | 15,920 |
| July | 10,000 | 15,920 |
| August | 13,000 | 16,880 |
| September | 14,000 | 18,080 |
| October | 18,000 | 19,280 |
| November | 20,000 | 21,200 |

Required

## Problem 5-1

Analyze mixed cost using high-low method and scatter diagram (L.O. 2)
a. Using the high-low method, determine the total amount of fixed costs and the amount of variable cost per unit. Draw the cost line.
b. Prepare a scatter diagram, plot the actual costs, and visually fit a linear cost line to the points. Estimate the amount of total fixed costs and the amount of variable cost per unit.

a. Using the preceding graph, label the relevant range, total costs, fixed costs, break-even point, and profit and loss areas.
b. At 8,000 units, what are the variable costs, fixed costs, sales, and contribution margin amounts in dollars?
c. At 8,000 units, is there net income or loss? How much?

The management of Bootleg Company wants to know the break-even point for its new line of hiking boots under each of the following independent assumptions. The selling price is $\$ 50$ per pair of boots unless otherwise stated. (Each pair of boots is one unit.)
a. Fixed costs are $\$ 300,000$; variable cost is $\$ 30$ per unit.
b. Fixed costs are $\$ 300,000$; variable cost is $\$ 20$ per unit.
c. Fixed costs are $\$ 250,000$; variable cost is $\$ 20$ per unit.
d. Fixed costs are $\$ 250,000$; selling price is $\$ 40$; and variable cost is $\$ 30$ per unit.

Compute the break-even point in units and sales dollars for each of the four independent cases.

Refer to Problem 5-3. Bootleg Company's sales are $\$ 1,100,000$. Determine the margin of safety in dollars for cases (a) through (d).

Using the data in Problem 5-3 ( a through d ), determine the level of sales dollars required to achieve a net income of $\$ 125,000$.

Problem 5-2
Identify points on a cost-volume-profit chart (L.O. 3)

Problem 5-3
Determine break-even point under varying assumptions
(L.O. 3, 4)

Problem 5-4
Determine the margin of safety (L.O. 5)

Problem 5-5
Compute the level of sales dollars needed to achieve a specified
level of income (L.O. 6)

Problem 5-6 Compute multiproduct break-even point
(L.O. 4)

Bikes Unlimited, Inc., sells three types of bicycles. It has fixed costs of $\$ 258,000$ per month. The sales and variable costs of these products for April follow:

| Racing | Mountain | Touring |
| ---: | ---: | ---: |
| $\$ 1,000,000$ | $\$ 1,500,000$ | $\$ 2,500,000$ |
| 700,000 | 900,000 | $1,250,000$ |

Required

## Problem 5-7

Applying cost-volumeprofit analysis to various situations (L.O. 6)

Compute the break-even point in sales dollars.
a. Assume that fixed costs of Celtics Company are $\$ 180,000$ per year, variable cost is $\$ 12$ per unit, and selling price is $\$ 30$ per unit. Determine the break-even point in sales dollars.
b. Hawks Corporation breaks even when its sales amount to $\$ 89,600,000$. In 1997, its sales were $\$ 14,400,000$, and its variable costs amounted to $\$ 5,760,000$. Determine the amount of its fixed costs.
c. The sales of Niners Corporation last year amounted to $\$ 20,000,000$, its variable costs were $\$ 6,000,000$, and its fixed costs were $\$ 4,000,000$. At what level of sales dollars would the Niners Corporation break even?
d. What would have been the net income of the Niners Corporation in part ( c ), if sales volume had been $10 \%$ higher but selling prices had remained unchanged?
e. What would have been the net income of the Niners Corporation in part (c), if variable costs had been $10 \%$ lower?
f. What would have been the net income of the Niners Corporation in part ( c ), if fixed costs had been $10 \%$ lower?
g. Determine the break-even point in sales dollars for the Niners Corporation on the basis of the data given in (e) and then in (f).

Required $\rightleftharpoons$ Answer each of the preceding questions.
Problem 5-8
Compute break-even point and sales needed to achieve a specified level of income (L.O. 6)

Required 3

Problem 5-9
Prepare cost-volumeprofit chart; compute break-even point; prepare income statement for two companies
(L.O. 3, 4, 6)

Required 3

Problem 5-10
Compute break-even point; compute expected net income; make leasing decision (L.O. 4, 6)
a. Prepare a cost-volume-profit chart for Sierra Company, indicating the break-even point, the contribution margin, and the areas of income and losses.
b. Compute the break-even point of both companies in sales dollars and units.
c. Assume that without changes in selling price, the sales of each company decline by $10 \%$. Prepare income statements similar to the preceding statements for both companies.
After graduating from college, M. J. Orth started a company that produced cookbooks. After three years, Orth decided to analyze how well the company was doing. He discovered the company has fixed costs of $\$ 1,200,000$ per year, variable cost of $\$ 14.40$ per cookbook (on average), and a selling price of $\$ 26.90$ per cookbook (on average).

How many units (that is, cookbooks) must be sold to break even? How many units will the company have to sell to earn $\$ 48,000$ ?

The operating results for two companies follow:

|  | Sierra | Olympias |
| :--- | ---: | ---: |
| Sales $(20,000)$ units | $\$ 1,920,000$ | $\$ 1,920,000$ |
| Variable costs | 480,000 | $1,056,000$ |
| Contribution margin | $1,440,000$ | 864,000 |
| Fixed costs | 960,000 | 384,000 |
| Net income | 480,000 | 480,000 |

Soundoff, Inc., a leading manufacturer of electronic equipment, decided to analyze the profitability of its new portable compact disc (CD) players. On the CD player line, the company incurred $\$ 2,520,000$ of fixed costs per month while selling 20,000 units at $\$ 600$ each. Variable cost was $\$ 240$ per unit.

Recently, a new machine used in the production of CD players has become available; it is more efficient than the machine currently being used. The new machine would reduce the company's variable costs by $20 \%$, and leasing it would increase fixed costs by $\$ 96,000$ per year.
a. Compute the break-even point in units assuming use of the old machine.
b. Compute the break-even point in units assuming use of the new machine.
c. Assuming that total sales remain at $\$ 12,000,000$ and that the new machine is leased, compute the expected net income.
d. Should the new machine be leased? Why?

Surething CD Company reports sales of $\$ 720,000$, variable costs of $\$ 432,000$, and fixed costs of $\$ 108,000$. If the company spends $\$ 72,000$ on a sales promotion campaign, it estimates that sales will be increased by $\$ 270,000$.

Determine whether the sales promotion campaign should be undertaken. Provide calculations.
Problem 5-11 Decide whether to undertake a sales promotion campaign
(L.O. 6)

## ERequired

Problem 5-1A
Analyze a mixed cost using high-low method and scatter diagram (L.O. 2)

| Month | Units | Costs |
| :--- | ---: | ---: |
| January | 20,800 | $\$ 57,600$ |
| February | 20,000 | 54,000 |
| March | 22,000 | 58,500 |
| April | 25,600 | 57,600 |
| May | 28,400 | 58,500 |
| June | 30,000 | 62,100 |
| July | 32,000 | 63,900 |
| August | 35,600 | 68,400 |
| September | 37,600 | 72,000 |
| October | 40,000 | 77,400 |

a. Using the high-low method, determine the total amount of fixed costs and the amount of variable cost per unit. Draw the cost line.
b. Prepare a scatter diagram, plot the actual costs, and visually fit a linear cost line to the points. Estimate the amount of total fixed costs and the variable cost per unit.


Problem 5-2A
Identify points on a cost-volume-profit chart (L.O. 3)

Required

Problem 5-3A
Compute level of sales needed to break even and earn a specified level of income (L.O. 4)
a. Using the preceding graph, label the relevant range, total costs, fixed costs, break-even point, and profit and loss areas.
b. At 18,000 units, what would sales revenue, total costs, fixed and variable costs be?
c. At 18,000 units, would there be a profit or loss? How much?

Jefferson Company has a plant capacity of 100,000 units, at which level variable costs are $\$ 720,000$. Fixed costs are expected to be $\$ 432,000$. Each unit of product sells for $\$ 12$.

Required $\circlearrowleft$
a. Determine the company's break-even point in sales dollars and units.
b. At what level of sales dollars would the company earn net income of $\$ 144,000$ ?
c. If the selling price were raised to $\$ 14.40$ per unit, at what level of sales dollars would the company earn $\$ 144,000$ ?

Problem 5-4A
Determine break-even point under varying assumptions (L.O. 4)
a. Determine the break-even point in sales dollars and units for Cowboys Company that has fixed costs of $\$ 63,000$, variable cost of $\$ 24.50$ per unit, and a selling price of $\$ 35.00$ per unit.
b. Wildcats Company breaks even when sales are $\$ 280,000$. In March, sales were $\$ 670,000$, and variable costs were $\$ 536,000$. Compute the amount of fixed costs.
c. Hoosiers Company had sales in June of $\$ 84,000$; variable costs of $\$ 46,200$; and fixed costs of $\$ 50,400$. At what level of sales, in dollars, would the company break even?
d. What would the break-even point in sales dollars have been in ( c ) if variable costs had been $10 \%$ higher?
e. What would the break-even point in sales dollars have been in (c) if fixed costs had been $10 \%$ higher?
f. Compute the break-even point in sales dollars for Hoosiers Company in (c) under the assumptions of (d) and (e ) together.

Required
Answer each of the preceding questions.

## Problem 5-5A

Prepare cost-volumeprofit chart; compute break-even sales and sales needed to achieve a specified level of income (L.O. 3, 4, 6)

See Right Company makes contact lenses. The company has a plant capacity of 200,000 units. Variable costs are $\$ 4,000,000$ at $100 \%$ capacity. Fixed costs are $\$ 2,000,000$ per year, but this is true only between 50,000 and 200,000 units.

## Problem 5-6A

Compute break-even point in a multiproduct company (L.O. 4)
a. Prepare a cost-volume-profit chart for See Right Company assuming it sells its product for $\$ 40$ each. Indicate on the chart the relevant range, break-even point, and the areas of net income and losses.
b. Compute the break-even point in units.
c. How many units would have to be sold to earn $\$ 200,000$ per year?

Mr. Feelds Cookies has fixed costs of $\$ 360,000$ per year. It sells three types of cookies. The cost and revenue data for these products follow:

|  | Cookies |  |  |
| :--- | :---: | :---: | :---: |
|  | Cream | Goo | Sweet |
|  | Cake | Fill | Tooth |
| Sales | $\$ 64,000$ | $\$ 95,000$ | $\$ 131,000$ |
| Variable costs | 38,400 | 55,100 | 66,000 |

Compute the break-even point in sales dollars.

## Beyond the Numbers-Critical Thinking

Quality Furniture Company is operating at almost $100 \%$ of capacity. The company expects sales to increase by $25 \%$ in 2008 . To satisfy the demand for its product, the company is considering two alternatives: The first alternative would increase fixed costs by $15 \%$ but not affect variable costs. The second alternative would not affect fixed costs but increase variable costs to $60 \%$ of the selling price of the company's product.

This is Quality Furniture Company's condensed income statement for 2007:

| Sales | $\$ 3,600,000$ |  |
| :--- | ---: | ---: |
| Costs: | $\$ 1,620,000$ |  |
| $\quad$ Variable | 330,000 | $1,950,000$ |
| $\quad$ Fixed | $\underline{\$ 1,650,000}$ |  |
| Income before taxes | $\underline{y}$ |  |

a. Determine the break-even point in sales dollars for 2008 under each of the alternatives.
b. Determine projected income for 2008 under each of the alternatives.
c. Which alternative would you recommend? Why?

When the Weidkamp Company's plant is completely idle, fixed costs amount to $\$ 720,000$. When the plant operates at levels of $50 \%$ of capacity or less, its fixed costs are $\$ 840,000$; at levels more than $50 \%$ of capacity, its fixed costs are $\$ 1,200,000$. The company's variable costs at full capacity ( 100,000 units) amount to $\$ 1,800,000$.
a. Assuming that the company's product sells for $\$ 60$ per unit, what is the company's break-even point in sales dollars?
b. Using only the data given, at what level of sales would it be more economical to close the factory than to operate it? In other words, at what level would operating losses approximate the losses incurred if the factory closed down completely?
c. Assume that Weidkamp Company is operating at $50 \%$ of its capacity and decides to reduce the selling price from $\$ 60$ per unit to $\$ 36$ per unit to increase sales. At what percentage of capacity must the company operate to break even at the reduced sales price?

Monroe Company has recently been awarded a contract to sell 25,000 units of its product to the federal government. Monroe manufactures the components of the product rather than purchasing them. When the news of the contract was released to the public, President Mary Monroe, received a call from the president of the McLean Corporation, Carl Cahn. Cahn offered to sell Monroe 25,000 units of a needed component, Part J, for $\$ 15.00$ each. After receiving the offer, Monroe calls you into her office and asks you to recommend whether to accept or reject Cahn's offer.

Business Decision Case 5-1
Compute break-even point and projected net income for two investment alternatives; determine best alternative (L.O. 4, 6)

## Required

## Business Decision

 Case 5-2Compute break-even point; determine point at which factory should shut down rather than produce
(L.O. 4, 6)

## Business Decision

Case 5-3
Find variable cost and calculate cost to manufacture part; decide whether to buy a part (L.O. 3, 6)

You go to the company's records and obtain the following information concerning the production of Part J:

|  | Costs at Current <br> Production Level <br> $(\mathbf{2 0 0 , 0 0 0}$ units) |
| :--- | ---: |
| Direct labor | $\$ 1,248,000$ |
| Direct materials | 576,000 |
| Manufacturing overhead | 600,000 |
| Total cost | $\$ 2,424,000$ |

You calculate the unit cost of Part J to be $\$ 12.12$ or ( $\$ 2,424,000 \div 200,000$ ). But you suspect that this unit cost may not hold true at all production levels. To find out, you consult the production manager. She tells you that to meet the increased production needs, equipment would have to be rented and the production workers would work some overtime. She estimates the machine rental to be $\$ 60,000$ and the total overtime premiums to be $\$ 108,000$. She provides you with the following information:

> Costs at Current Production Level (225,000 units)

Direct labor Direct materials Manufacturing overhead (including equipmental rental and overtime premiums)
Total cost
\$1,404,000
648,000

828,000
\$2,880,000

Business Decision

## Case 5-4

Writing assignment (L.O. 4, 6)

## Group Project 5-5

Develop a cost-volume-profit equation for a new business (L.O. 3, 6, 7)

Refer to the "A Broader Perspective" discussion of cost-volume-profit analysis for television networks on page 148 . Write a memo to your instructor describing how the networks can reduce their break-even points.

In teams of two or three students, develop a cost-volume-profit equation for a new business that you might start. Examples of such businesses are a portable espresso bar, a pizza stand, a campus movie theater, a package delivery service, a campus-to-airport limousine service, and a T-shirt printing business.

Your equation should be in the form: Profits $=($ Price per unit $\times$ Volume $)-($ Variable cost per unit $\times$ Volume) - Fixed costs per period. Pick a period of time, say one month, and project the unit price, volume, unit variable cost, and fixed costs for the period. From this information, you will be able to estimate the profits-or losses-for the period. Select one spokesperson for your team to tell the class about your proposed business and its profits or losses. Good luck, and have fun.

Refer to "A Broader Perspective" discussion on page 143 of how cost-volume-profit analysis is used by colleges. In teams of two or three students, write a memo to your instructor defining step costs and explain why the step costs identified in the case are classified as such. Also include in your memo how the school might lower its break-even point.

In teams of two or three students, address the following questions:

- Why would a company consider increasing automation and decreasing the use of labor if the result would be an increase in the break-even point?
- Would an increase in automation increase fixed costs over the short-run, long-run, or both?

Write a memo to your instructor that addresses both questions. Be sure to explain your answers.

## Using the Internet-A View of the Real World

Visit the website for Intel Corporation, a high technology manufacturing company.
http://www.intel.com
Go to the company's most recent financial statements and review the consolidated statement of income. What additional information, if any, would you need to perform cost-volume-profit analysis? Why is this information excluded from Intel's income statement?

Visit the website for Wal-Mart Corporation, a retail company.

## http://www.walmart.com

Group Project 5-6 Writing assignment

Group Project 5-7 Writing assignment

Go to the company's most recent financial statements and review the statement of income. What additional information, if any, would you need to perform cost-volume-profit analysis? Why is this information excluded from Wal-Mart Corporation's income statement?


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## Answers to Self-Test

## True-False

1. False. The high-low method is less precise than the scatter diagram because it requires only two data points in the computation.
2. False. The break-even point can also be expressed in units produced or sold.
3. False. Total contribution margin is the amount by which revenue exceeds variable costs of producing that revenue.

## Multiple-Choice

1. c. Electricity is a mixed cost.
2. d. Step costs have all of these characteristics-a fixed component, costs increase, and constancy over a relevant range for a step.
3. c.

$$
\begin{aligned}
\mathrm{BE}_{\text {dollars }} & =\frac{\text { Fixed costs }}{\text { Contribution margin ratio }} \\
\text { Contribution margin ratio } & =(\$ 10-\$ 6) / \$ 10=0.40 \\
\mathrm{BE}_{\text {dollars }} & =\frac{\$ 20,000}{0.40}=\$ 50,000
\end{aligned}
$$

4. a. Contribution margin $=$ Selling price Variable costs

$$
=\$ 20-\$ 6=\$ 14
$$

4. False. Margin of safety $=$ Current sales -Break-even sales.
5. True. Dollars of sales are used as the measure of volume when a company has many different products.
6. d.

$$
\begin{aligned}
& \mathrm{BE}_{\text {units }}=\frac{\text { Fixed costs }}{\text { Contribution margin }} \\
& \begin{aligned}
\text { per unit }
\end{aligned} \\
& \mathrm{BE}_{\text {units }}=\frac{\$ 28,000}{\$ 14 \text { per unit }} \\
&=2,000 \text { units }
\end{aligned}
$$

6. d. All of these are assumptions-prices and costs remain constant through the relevant range, product mix is known, and costs can be accurately classified into fixed and variable components.

[^0]:    ${ }^{1}$ A more sophisticated and precise method, called the least squares method, could be used to draw the regression line. This method involves statistical analysis and is beyond the scope of this text.

[^1]:    All loans ara subject to spplication and credit spproval
     annuef cost of attencance exceeds $\$ 30,000$ ). Briowers in Une Continuing Educallon loan prograth may borrow annually up lo $\$ 30,000$
     options also avallable
    ${ }^{\text {tr }} \mathrm{A} .0 .25 \%$ interest rate reduction is avallable for borrowers who olect to have monthiy principal and interest payments fransferred olectronically from a savings or checkino account. The interest rate reduction will begin when automatic pricipal and interest payments stant, and will remain in aflect as long as automatic payments continue witnout ofernuption This reducac
     rate reduction it (1) the first 36 payments of principal and interest are pair on time and (2) at any time prior to the 36 th on timie payment, the porrower whio recalves the morthly bill elects 10 have rnonthly principat and interest paynents transterred electroncally from a savings or cheoking account and continues to make such automatic paymenta through the 36 th payment
    
    
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