

$$a) \quad OA + AB = OB$$

$$\Rightarrow AB = OB - OA$$

$$\Rightarrow \underline{AB = \vec{b} - \vec{a}}$$

$$b) \quad OA:AC = 1:3$$

$$\Rightarrow \frac{OA}{AC} = \frac{1}{3}$$

$$\Rightarrow 3OA = AC$$

$$\text{OR } AC = 3OA$$

$$\text{But } OA = \vec{a}$$

$$\Rightarrow \underline{AC = 3\vec{a}}$$

$$c) \quad OD = 4OB$$

$$\text{but } OB = \vec{b}$$

$$\underline{OD = 4\vec{b}}$$

$$\text{Now, } OC + CD = OD$$

$$CD = OD - OC \\ = 4\vec{b} - OC$$

$$\text{Also } OC = OA + AC \\ = \vec{a} + 3\vec{a}$$

$$OC = 4\vec{a}$$

$$\underline{CD = 4\vec{b} - 4\vec{a}}$$

$$d) \quad AB = \vec{b} - \vec{a}$$

$$CD = 4\vec{b} - 4\vec{a} \\ = 4(\vec{b} - \vec{a})$$

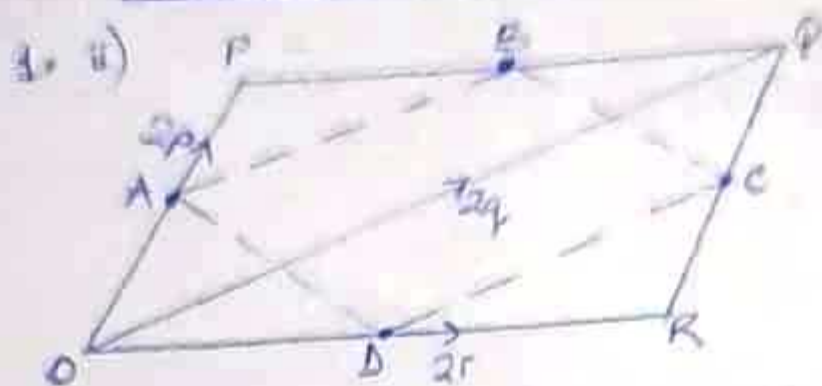
$$CD = 4AB$$

CD is a scalar multiple of AB

CD and AB are parallel. Also

CD and AB have the same direction vector $\vec{b} - \vec{a}$. Hence parallel.

SOLUTIONS OF EXERCISES



$$BQ = \frac{1}{2}(PQ)$$

$$= \frac{1}{2}(2q - 2r)$$

$$\underline{BQ = q - r}$$

$$CQ = \frac{1}{2}(RQ)$$

$$= \frac{1}{2}(2q - 2r)$$

$$\underline{CQ = q - r}$$

a) $OA = \frac{1}{2}OP$

$$OA = \frac{1}{2}(2p)$$

$$\Rightarrow \underline{OA = p}$$

b) $OP + PQ = OQ$

$$PQ = OQ - OP$$

$$\underline{PQ = 2q - 2p}$$

But $PB = \frac{1}{2}PQ$

$$\Rightarrow PB = \frac{1}{2}(2q - 2p)$$

$$\Rightarrow \underline{PB = q - p}$$

c) $AB = AP + PB$

$$= p + q - p$$

$$\Rightarrow \underline{AB = q}$$

d) $OR = \frac{1}{2}OP$

$$\Rightarrow OR = \frac{1}{2}(2r)$$

$$\Rightarrow \underline{OR = r}$$

e) $RQ = OQ - OR$

$$\Rightarrow \underline{RQ = 2q - 2r}$$

$$RC = \frac{1}{2}RQ$$

$$= \frac{1}{2}(2q - 2r)$$

$$\Rightarrow \underline{RC = q - r}$$

f) $DC = DR + RC$

$$= r + q - r$$

$$\Rightarrow \underline{DC = q}$$

ii) $AB = DC = q$ It follows that AB is parallel to DC .

AD is parallel to BC . $AD = OD + AO = r + p$

$BC = BQ - CQ = (q - p) - (q - r) = r + p$

$ABCD$ is a parallelogram

$$\underline{= r + p}$$